

Luck-Adjusted Pitching Statistics
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Attempting to forecast players' performances causes headaches, despite the many theories around on what contributes to ERA, WHIP and Wins. Linear prediction systems such as FIP Era are on the right track, but there is a deeper level of causal effects at work. Any forecasting system should be able to predict player performance based on as much luck-independent information as possible.

FIP Era is calculated as $(HR*13+(BB+HBP-IBB)*3-K*2)/IP + 3.2$. This is a rough parametrization of the effects of BB, HBP, IBB, K and IP on ERA, but is not estimated in any statistical sense. Also, FIP Era ignores useful information on the type of contact pitchers tend to induce beyond HRs, reflected in BABIP, and the strand rate of runners the pitcher allows. Like FIP Era, I try to estimate ERA using only the statistics that the pitcher can presumably control and that are readily accessible, but I also add more information by using additional statistics. To estimate ERA, luck-adjusted statistics first need to be computed; in particular BABIP, LOB%, and HR/9.

There are three statistics that are related to luck more than anything, BABIP, LOB%, and the number of HRs a pitcher gives up over the course of a season. These statistics are considered here to be the only causes of randomness for pitchers. Once these are estimated, luck-adjusted WHIP, ERA, and Wins is estimated using similar methods. At each step of the way, interesting pieces of information are uncovered that reveal a clearer picture of what determines a pitcher's success.

Below are the summary statistics for the dataset of pitchers being analyzed.

Variable	Obs	Mean	Std. Dev.	Min	Max
babip	126	.3034921	.0235735	.24	.37
lob	126	72.02778	4.664412	61.1	84.4
gb	126	43.74603	6.776355	22	64
fb	126	35.92619	6.214707	20.4	53.4
iffb	126	9.706349	2.97205	4	19
k9	126	6.568492	1.585725	3.35	11.01
bb9	126	3.027936	.9407021	1.35	5.98
hr9	126	1.01746	.3001784	.44	1.94
teamruns	126	4.590079	.3899877	3.86	5.46
era	126	4.239365	.9498427	2.07	6.66
whip	126	1.357857	.1688057	1	1.8
w32	126	12.02906	3.574368	4.363636	22.70968

The sample includes 126 pitchers in 2008 with more than 100 innings and no more than 5 relief appearances. Average BABIP is 0.303, average LOB% is 72%, 43% of all hit balls are ground balls, and so on. W32 is the number of wins normalized over 32 starts. Teamruns is the average number of runs per game the pitcher's team scores over the course of the regular season.

In every estimation, general specifications are attempted first, using all potentially relevant, luck-independent variables. The estimates reported are the final, parsimonious regressions and these can be considered the best estimates of a change in a right-hand-side variable on the left-hand-side variable.

First, I estimate a model for a pitcher's BABIP.

$$\text{BABIP} = A1 + A2 * \text{GB}\% + A3 * \text{FB}\% + A4 * \text{IFFB}\% + EA$$

Source	SS	df	MS	Number of obs = 126		
Model	.017682096	3	.005894032	F(3, 122)	=	13.89
Residual	.0517814	122	.000424438	Prob > F	=	0.0000
Total	.069463495	125	.000555708	R-squared	=	0.2546
				Adj R-squared	=	0.2362
				Root MSE	=	.0206

babip	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
gb	-.0043473	.0008444	-5.15	0.000	-.0060188	-.0026757
fb	-.0053375	.0009242	-5.78	0.000	-.0071671	-.0035079
iffb	-.0011018	.0006985	-1.58	0.117	-.0024846	.0002809
_cons	.6961184	.0691862	10.06	0.000	.5591573	.8330794

Where EA is a stochastic error term. These results show that GB%, FB%, and IFFB% explain about 25% of the variation in BABIP from pitcher to pitcher and indicate that BABIP is fairly random. An increase of 1% in GB% decreases the estimated BABIP of a pitcher by -0.0043 (other estimates are interpreted similarly). Therefore, a difference of 5% in GB% will result in a change in BABIP for a league average pitcher from .303 to about .323. Using these parameter estimates, I estimate a luck-adjusted BABIP as

$$\begin{aligned} \text{aBABIP} &= A1 + A2 * \text{GB}\% + A3 * \text{FB}\% + A4 * \text{IFFB}\% \\ \text{aBABIP} &= 0.696 - 0.00110 * \text{GB}\% - 0.005 * \text{FB}\% - 0.00434 * \text{IFFB}\% \end{aligned}$$

Next, I estimate a luck-adjusted LOB%.

$$\text{LOB}\% = B1 + B2 * \text{K9} + B3 * \text{BABIP} + EB$$

Source	SS	df	MS	Number of obs = 126		
Model	1275.67491	2	637.837453	F(2, 123)	=	54.33
Residual	1443.91758	123	11.7391673	Prob > F	=	0.0000
Total	2719.59249	125	21.7567399	R-squared	=	0.4691
				Adj R-squared	=	0.4604
				Root MSE	=	3.4262

lob	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
k9	1.419747	.1933051	7.34	0.000	1.037111	1.802382
babip	-98.2937	13.00313	-7.56	0.000	-124.0326	-72.55481
_cons	92.53354	4.129896	22.41	0.000	84.35867	100.7084

Perhaps surprisingly, 46% of the pitcher to pitcher variation in LOB% can be explained just by the pitchers K/9 rate and its BABIP. An additional K/9 reduces the LOB% of a pitcher by 1.4%. Also, and more importantly, a .001 increase in BABIP reduces LOB% by 0.98%. This means that bad luck not only gets runners on base, it helps them to score. Therefore, rather than estimate a LOB% with BABIP

to calculate luck-adjusted LOB%, I use the aBABIP previously estimated to control for a lucky BABIP.

$$aLOB\% = B1 + B2 * K9 + B3 * aBABIP$$

I can also estimate the number of home runs per 9 innings as a function of the fly ball % and the number of strike outs per 9 innings.

$$HR9 = C1 + C2 * FB\% + C3 * K9 + EC$$

Source	SS	df	MS			
Model	3.70082823	2	1.85041411	Number of obs =	126	
Residual	7.56255914	123	.061484221	F(2, 123) =	30.10	
Total	11.2633874	125	.090107099	Prob > F =	0.0000	
				R-squared =	0.3286	
				Adj R-squared =	0.3177	
				Root MSE =	.24796	

hr9	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
k9	-.075395	.0146186	-5.16	0.000	-.1043317 -.0464584
fb	.0262808	.00373	7.05	0.000	.0188974 .0336641
_cons	.5685244	.1420498	4.00	0.000	.2873455 .8497034

A high strikeout rate and low FB% both reduce the frequency of surrendering home runs. Clearly, park factors also contribute to the frequency of HRs allowed, but these are omitted in this analysis. Luck-adjusted HR9 can be estimated as:

$$aHR9 = C1 + C2 * FB\% + C3 * K9 + EC$$

and the estimated number of home runs surrendered over the course of a season as

$$aHR = aHR9 * IP / 9$$

From aHR and aBABIP, estimated hits can also be calculated by

$$aH = aBABIP / BABIP * (H - HR) + aHR$$

and an estimated WHIP can be calculated as

$$aWHIP = (BB + aH) / IP$$

Next, ERA can be estimated by

$$ERA = D1 + D2 * LOB\% + D3 * K9 + D4 * BB9 + D5 * BABIP + D6 * HR9 + ED$$

Source	SS	df	MS			
Model	108.36269	5	21.6725381	Number of obs =	126	
Residual	4.41246267	120	.036770522	F(5, 120) =	589.40	
				Prob > F =	0.0000	
				R-squared =	0.9609	

Total	112.775153	125	.902201224					Adj R-squared = 0.9592	Root MSE = .19176
era	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]				
lob	-.0944805	.0051727	-18.27	0.000	-.1047222	-.0842389			
k9	-.1243317	.0136964	-9.08	0.000	-.1514497	-.0972137			
bb9	.3139747	.0191164	16.42	0.000	.2761257	.3518238			
babip	11.02971	.8819844	12.51	0.000	9.283445	12.77598			
hr9	1.324773	.0591788	22.39	0.000	1.207603	1.441943			
_cons	6.215228	.544756	11.41	0.000	5.136649	7.293806			

This equation predicts an astonishing 96% of the pitcher-to-pitcher variation in ERA. Put another way, values for LOB%, K9, BB9, BABIP, and HR9, ERA can be predicted with 96% accuracy. The randomness with ERA therefore lies within the components of these 5 variables. Again, looking at the “luck” variables, an increase in LOB% reduces ERA by 0.09 and an increase in babip of .001 increases ERA by .01. Luck-adjusted ERA is predicted using the same method as aBABIP, aLOB, and aHR9

$$aERA = D1 + D2 * aLOB\% + D3 * K9 + D4 * BB9 + D5 * aBABIP + D6 * aHR9$$

Wins per 32 games started is estimated using the model

$$W32 = E1 + E2 * ERA + E3 * RF + EE$$

Source	SS	df	MS	Number of obs = 126		
Model	750.475191	2	375.237596	F(2, 123) = 54.52		
Residual	846.537934	123	6.88242222	Prob > F = 0.0000		
Total	1597.01312	125	12.776105	R-squared = 0.4699		
				Adj R-squared = 0.4613		
				Root MSE = 2.6234		
w32	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
era	-2.474227	.2475097	-10.00	0.000	-2.964157	-1.984297
teamruns	2.188119	.6028275	3.63	0.000	.9948587	3.381379
_cons	12.47458	2.907535	4.29	0.000	6.719287	18.22986

where RF, also called “teamruns” is the average runs the pitchers' team scores per game in all games it plays during the regular season for that year. A 1 point increase in ERA reduces the predicted number of games won by 2.47 over 32 starts. An increase of 1 average run per game for the pitchers team increases the number of wins by 2.1 over 32 starts.

and predicted as

$$aW32 = E1 + E2 * aERA + E3 * RF$$

and normalized luck-adjusted Wins are calculated,

$$aW = aW32 * Starts$$

Now that all of these new fancy luck-adjusted statistics have been created, who were the lucky and unlucky guys last year? How good is FIP Era?

FIP Era and aERA are naturally similar when the underlying luck-dependent statistics are close to the luck-independent statistics. However, in cases where a pitcher has luck-independent statistics that are farther away from the average for all pitchers, aERA and FIP Era diverge. By definition, since aERA is estimated using a minimum variance estimator, it is better at estimating within-season performance. In terms of forecasting, these two methods can be evaluated comparing actual to predicted statistics for years out-of-sample. This has not yet been done, but is necessary to establish which system has the better forecasting performance.